

Factor Completely:

1.  $18x^3y^2 - 10x^2 + 24y$

$2(9x^3y^2 - 5x^2 + 12y)$

2.  $x^3 + 2x^2 - 48x$

$x(x^2 + 2x - 48)$   
 $(x^2 - 6x)(8x - 48)$   
 $x(x-6)(8)(x-6)$   
 $x(x+8)(x-6)$

$a=1$   
 $b=2$   
 $c=-48$   
 $ac=-48$   

-2	24
-3	16
-4	12
-6	8

3.  $5m^2 + 30m - 35$

$5(m^2 + 6m - 7)$   
 $(m^2 + 7m)(m - 7)$   
 $m(m+7) - 1(m+7)$   
 $5(m-1)(m+7)$

$ac = \frac{-7}{7|-1}$

4.  $x^2 - 14xy - 51y^2$

$(x^2 - 17xy)(3xy - 51y^2)$   
 $x(x-17y)(3y)(x-17y)$   
 $(x+3y)(x-17y)$

$a=1$   
 $b=-14$   
 $c=-51$   
 $ac = \frac{-51}{-7|3}$

# Factoring Polynomials

## DIFFERENCE OF SQUARES

Review! Simplify the following:

- $(x + 4)(x - 4) = \underline{x^2 - 4x + 4x - 16} = \underline{x^2 - 16}$
- $(5x + 1)(5x - 1) = \underline{25x^2 - 5x + 5x - 1} = \underline{25x^2 - 1}$
- $(2a + 3b)(2a - 3b) = \underline{4a^2 - 6ab + 6ab - 9b^2} = \underline{4a^2 - 9b^2}$

↑  
This resulting product is called  
a DIFFERENCE OF SQUARES.

To factor a difference of squares, use the following rule:

$$a^2 - b^2 = (a-b)(a+b)$$

**Examples:** Factor the following difference of squares. *Check your answers by FOIL.*

1.  $a^2 - 4$

$$(a-2)(a+2)$$

2.  $n^2 - 64$

$$(n-8)(n+8)$$

3.  $81 - x^2$

$$(9-x)(9+x)$$

4.  $c^2 - 100$

$$(c-10)(c+10)$$

5.  $k^2 + 25$

PRIME

6.  $1 - 49y^2$

$$(1-7y)(1+7y)$$

7.  $9b^2 - 100$

$$(3b-10)(3b+10)$$

8.  $25x^2 - 49$

$$(5x+7)(5x-7)$$

9.  $16a^2 - 121$

$$(4a-11)(4a+11)$$

10.  $x^2 - 81y^2$

$$(x-9y)(x+9y)$$

11.  $4h^2 - 25g^2$

$$(2h+5g)(2h-5g)$$

12.  $64u^2 - v^2$

$$(8u-v)(8u+v)$$

Sometimes you have to take out the GCF first including variables in order to have a Difference of Squares.

Example:

$$48a^3 - 12a$$

$$\text{GCF} = 12a$$

$$12a(4a^2 - 1)$$

$$12a(2a-1)(2a+1)$$

When you write your final answer the GCF goes outside your two ( )

<p>21. <math>24a^2 - 54b^2</math></p>	<p>22. <math>36x^3 - 9x</math></p>
<p>23. <math>45q^3 - 20q</math></p>	<p>24. <math>32s^2 - 18u^2</math>  <math>2(16s^2 - 9u^2)</math>  <math>2(4s - 3u)(4s + 3u)</math></p>
<p>25. <math>100b^3 - 36b</math></p>	<p>26. <math>3x^4 - 48x^2</math>  <math>3x^2(x^2 - 16)</math>  <math>3x^2(x - 4)(x + 4)</math></p>
<p>27. <math>8x^2y - 32y^3</math>  <math>8y(x^2 - 4y^2) = 8y(x - 2y)(x + 2y)</math></p>	<p>28. <math>125m^3 - 5m</math></p>
<p>29. <math>3n^2 - 147</math></p>	<p>30. <math>18x^2 - 50</math></p>