

1. Complete the table:

<u>Characteristic</u>	<u>How to prove</u>
Parallel Lines	Same slope
Perpendicular Lines (Right angles)	Opposite reciprocal Slope
Side length	1. distance 2. Pythagorean theorem

2. Given the points (10, 4) and (14, -3)

A. Find the midpoint

$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$\left(\frac{10 + 14}{2}, \frac{4 + (-3)}{2} \right)$$

$$\left(12, \frac{1}{2} \right)$$

B. Find the distance

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\sqrt{(14 - 10)^2 + (-3 - 4)^2}$$

$$\sqrt{4^2 + (-7)^2}$$

$$\sqrt{16 + 49}$$

$$d = \sqrt{65}$$

WHAT IS IT

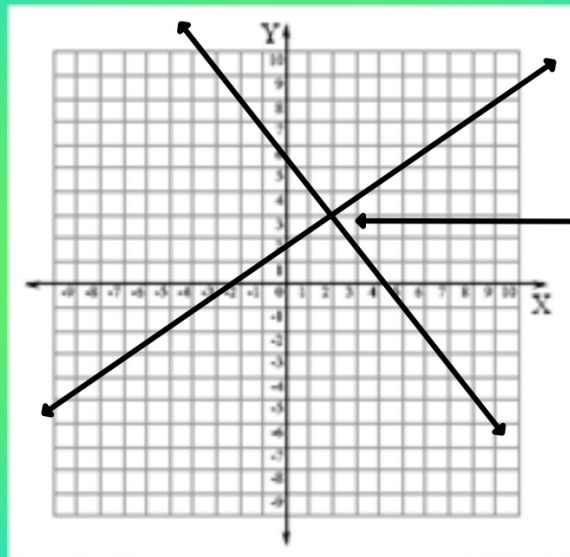
Two or more linear equations involving the same variables form a system of equations.

A solution of the system of equations is an ordered pair that satisfies *both* equations.

Systems of Equations

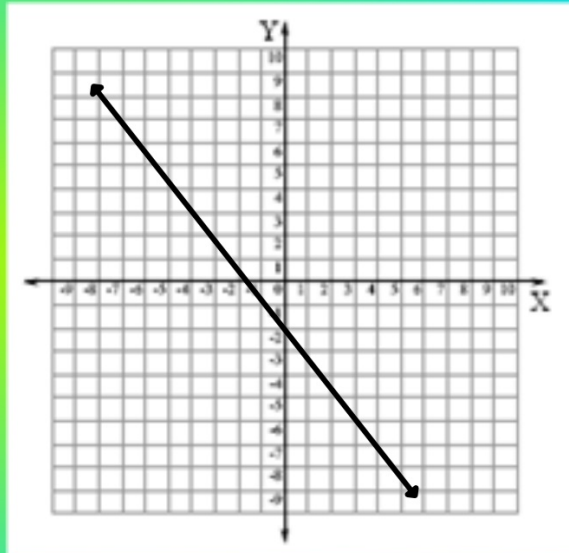
GRAPHING
METHOD

Two intersecting lines will have 1 solution.



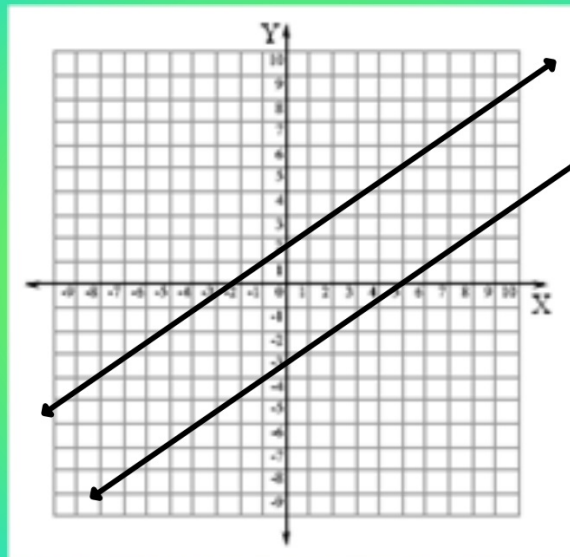
(x, y)

Two lines that are the same will have infinitely many solutions.



(The lines are on top of each other)

Two parallel lines will have no solution.



(They never intersect)

Graphing Method

WHEN TO USE??

...when both equations are in slope-intercept form ($y=mx+b$)

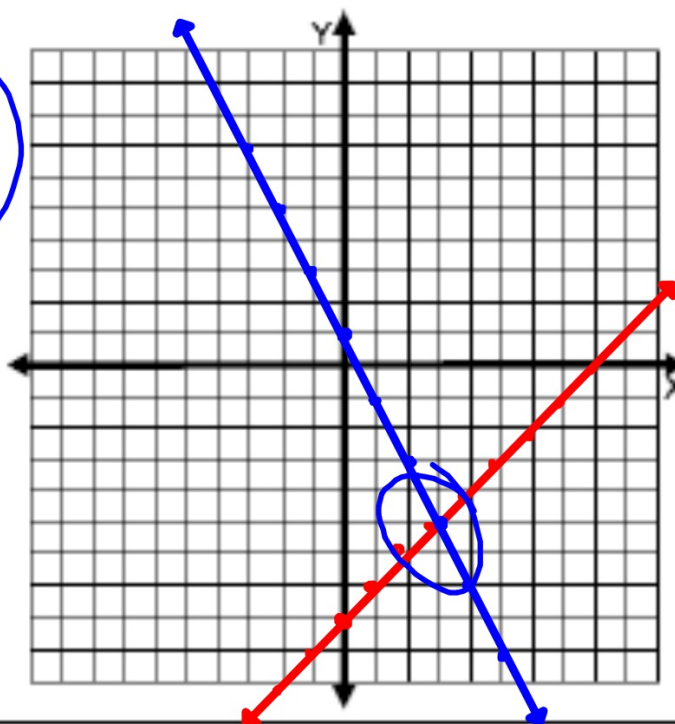
Ex: $y = x + 3$
 $y = x - 1$

Solving by Graphing

Note: Make sure equations are in **Slope-intercept** form!

1. $y = x - 8$
 $y = -2x + 1$

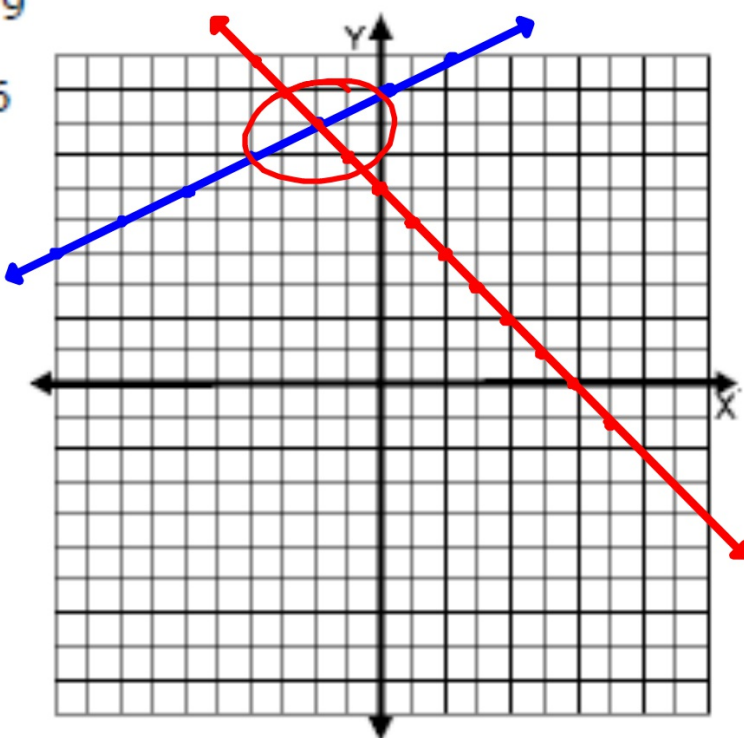
$(3, -5)$



$$2. y = \frac{1}{2}x + 9$$

$$y = -x + 6$$

$(-2, 8)$

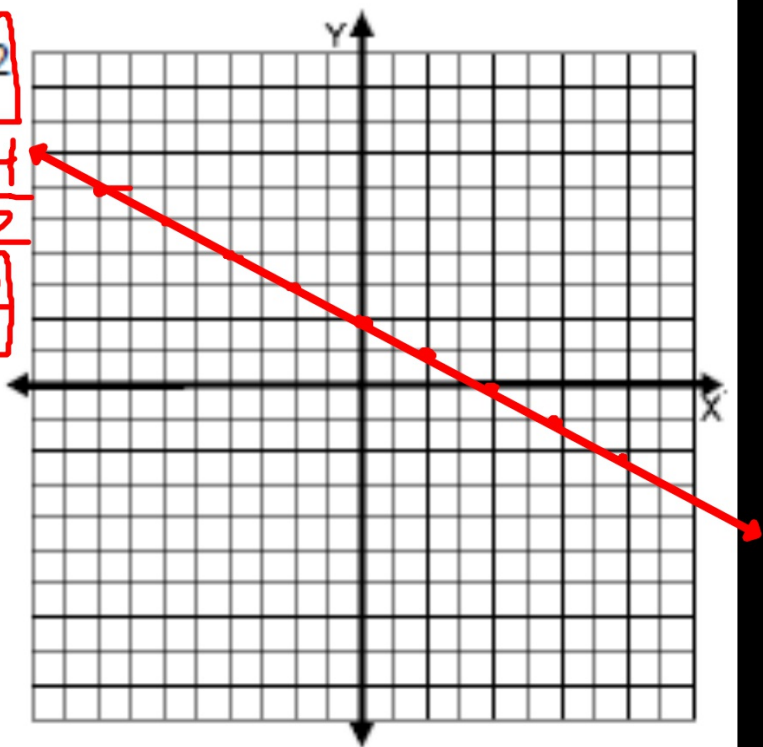


$$4. x + 2y = 4$$

$$y = -\frac{1}{2}x + 2$$

$$\frac{2y}{2} = \frac{-x+4}{2}$$

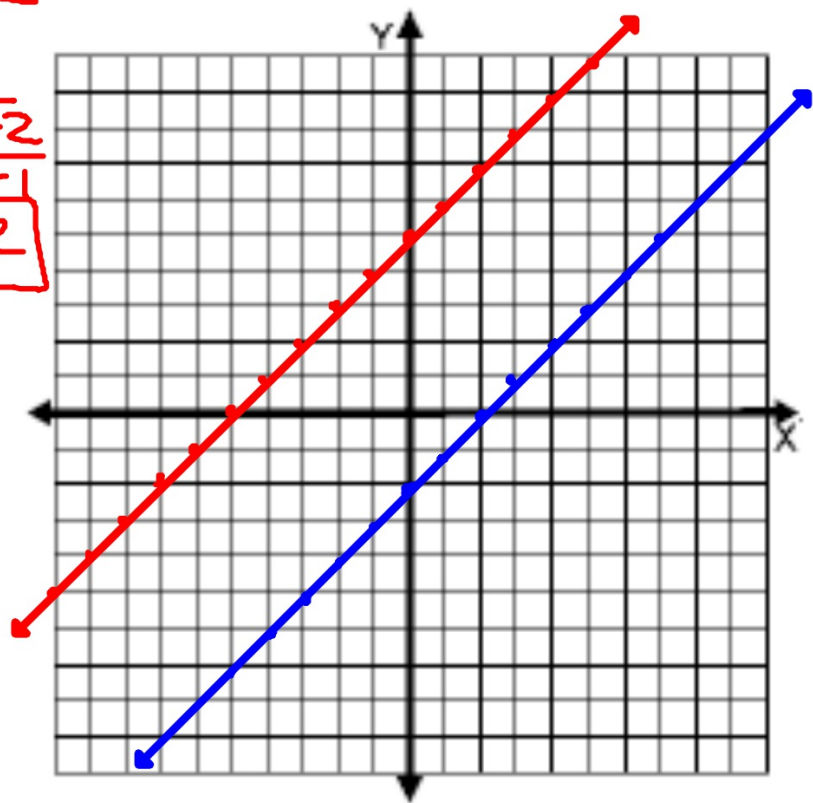
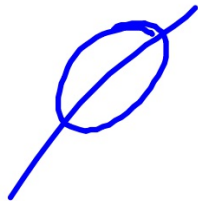
$$y = -\frac{1}{2}x + 2$$



6. $y = x + 5$

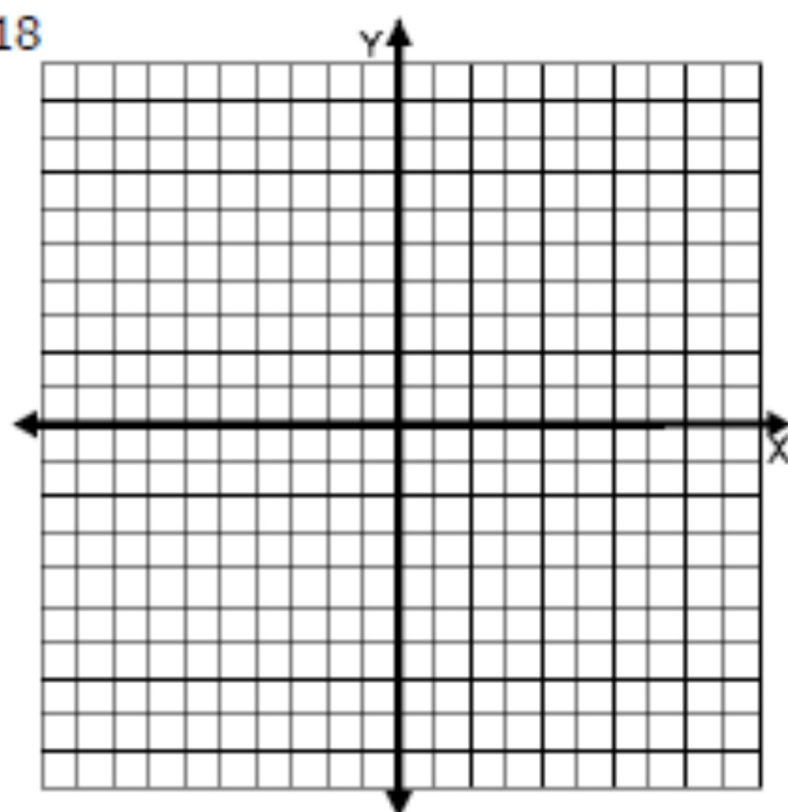
$$\begin{array}{r} x - y = 2 \\ -x \quad -x \\ \hline -y = -x + 2 \\ -1 \quad -1 \quad -1 \end{array}$$

$y = x - 2$



8. $x = -2$

$3x - 2y = -18$



SUBSTITUTION METHOD

STEPS TO SOLVE

1. Solve one equation for x or y
2. Plug in this expression into the other equation and Solve for the variable.
3. Plug in your answer into the revised equation from Step 1 and Solve for the other variable.

Substitution Method

$$y = 6x$$

$$y = 6(-1) \quad (-1, -6)$$

$$2x + 3y = -20$$

$$2x + 3(6x) = -20$$

$$2x + 18x = -20$$

$$\frac{20x}{20} = \frac{-20}{20}$$

$$x = -1$$

Substitution Method

$$(3, -1)$$

$$x = 4y + 7$$

$$2x - 6y = 12$$

$$x = 4(-1) + 7$$

$$x = -4 + 7$$

$$2(4y + 7) - 6y = 12$$

$$x = 3$$

$$8y + 14 - 6y = 12$$

$$2y + 14 = 12$$
$$\quad -14 \quad -14$$

$$\frac{2y}{2} = \frac{-2}{2}$$

$$y = -1$$

Is one equation solved for a specific variable

Substitution Method

(2, 5)

$$2x - 3y = -11$$

$$\begin{array}{r} 2x + y = 9 \\ -2x \quad -2x \\ \hline y = -2x + 9 \end{array}$$

$$\begin{array}{r} 2(2) + y = 9 \\ 4 + y = 9 \\ -4 \quad -4 \\ \hline y = 5 \end{array}$$

$$2x - 3(-2x + 9) = -11$$

$$2x + 6x - 27 = -11$$

$$8x - 27 = -11$$

$$\begin{array}{r} +27 \quad +27 \\ \hline 8x = 16 \end{array}$$

$$\frac{8x}{8} = \frac{16}{8} \quad x = 2$$

Is one equation (or both) solved for a

Steps for Solving by Graphing

Step 1: Enter the equations in the $y=$ screen

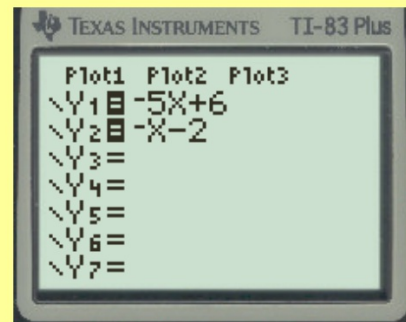
Step 2: **Graph** the equations. Use a standard graphing window(**ZOOM 6**)

Step 3: Use the **calc** feature(**2nd Trace**). Choose **intersect** to find the point where the lines intersect.

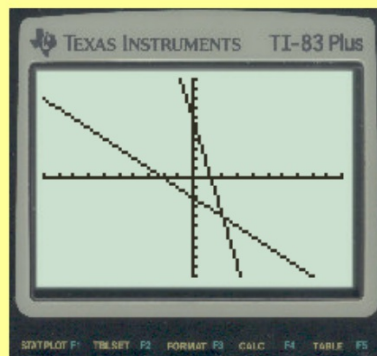
Step 4: Record your answer as (x, y)

Example 1: $y = -5x + 6$
 $y = -x - 2$

Step 1: Enter the equation in **y=**

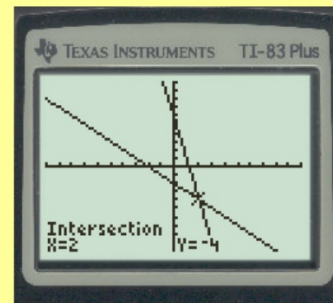


Step 2: Graph using the standard window...**Zoom #6**



Step 3: Use the **Calc** feature. Choose **Intesect** to find the point where the lines intersect.

*Note: You will need to hit **ENTER** three times until you see the words **INTERSECTION**!



Step 4: Record your answer as (x,y)

Solution: (2, -4)