

1. Simplify:  $(2x-2)^2$

$$\begin{array}{r} 2x - 2 \\ \hline 2x \quad 4x^2 \quad -4x \\ -2 \quad -4x \quad 4 \\ \hline \end{array} \quad \boxed{4x^2 - 8x + 4}$$

2. Factor completely:  $y^2 + 2y - 35$   $a=1$   $b=2$   $c=-35$

$$\begin{aligned} & (y^2 + 7y)(5y - 35) \\ & \textcircled{y} \textcircled{y+7} \textcircled{-5} \textcircled{y+7} \\ & \boxed{(y-5)(y+7)} \end{aligned} \quad \begin{aligned} & ac = -35 \\ & \quad \quad \quad \underline{7 \quad -5} \end{aligned}$$

3. Tickets to a movie cost \$7.25 for an adult and \$5.50 for students. A group of friends purchased 8 tickets for \$52.75. How many adult tickets and how many student tickets were purchased?

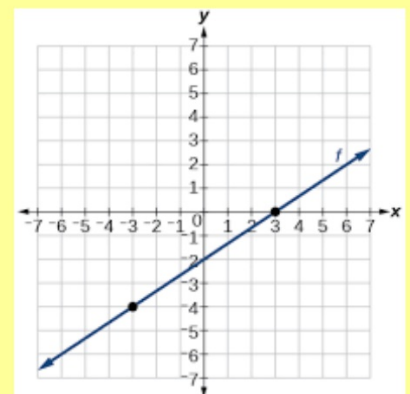
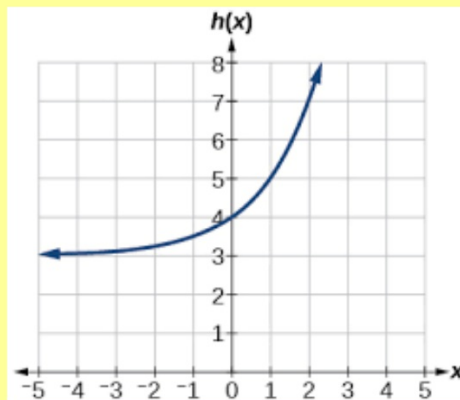
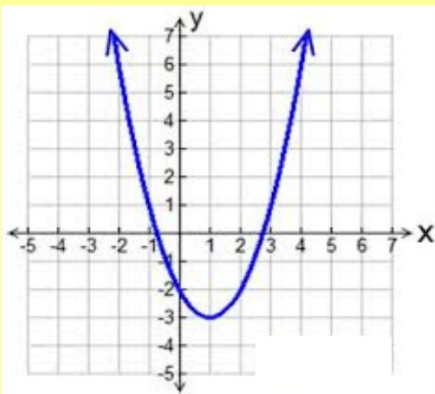
$x =$  adult tickets  $y =$  student tickets

$$\begin{aligned} & -7.25(x+y=8) \\ & \quad \quad \quad \underline{7.25x + 5.50y = 52.75} \\ + & \quad \quad \quad \underline{-7.25x - 7.25y = -58} \\ & \quad \quad \quad \underline{-1.75y = -5.25} \\ & \quad \quad \quad \underline{-1.75} \quad \quad \underline{-1.75} \\ & \quad \quad \quad y = 3 \end{aligned}$$

4. Solve for r:

$$\begin{aligned} & A = \pi r^2 \\ & \frac{A}{\pi} = \frac{\pi r^2}{\pi} \\ & \sqrt{\frac{A}{\pi}} = \sqrt{r^2} \\ & r = \sqrt{\frac{A}{\pi}} \end{aligned}$$

# Linear versus Non-Linear Functions



## Identifying from an equation...

### Linear

#### Standard form

$$y = mx + b$$

Has a variable with no exponent

#### Examples

$$y = -4x - 20$$

$$y = \frac{1}{2}x + 3$$

$$2x + y = 14$$

### Exponential

$$y = a(b)^x$$

The exponent is the variable

$$y = 10(2)^x$$

$$y = 7\left(\frac{1}{2}\right)^x$$

$$y = 3^x$$

### Quadratic

$$y = ax^2 + bx + c$$

Has a variable squared  
(To the second power)

$$y = -16x^2 + 8x - 2$$

$$y = 2x^2 - 4x + 1$$

$$y = -x^2 + 8$$

Identify as "increasing linear", "decreasing linear", "exponential growth", "exponential decay", "positive quadratic" or "negative quadratic"

$$y = 2(1.05)^x \quad \underline{\text{exp. growth}}$$

$$y = -3x^2 + 5x - 1 \quad \underline{\text{neg. quadratic}}$$

$$y = -8x + 20 \quad \underline{\text{dec. linear}}$$

$$y = 5x - 9 \quad \underline{\text{inc. linear}}$$

$$y = x^2 + 4x + 3 \quad \underline{\text{pos. quadratic}}$$

$$y = 3(0.8)^x \quad \underline{\text{exp decay}}$$

## Identifying from a Table...

### Linear

Look for  
a constant  
rate of  
change  
(Adding or  
Subtracting)

COMMON  
DIFFERENCE

### Exponential

Look for a  
constant  
rate of change  
(Multiplying)

COMMON  
RATIO

### Quadratic

Look for  
symmetry  
in the y-values

Pattern with the  
second difference

### **Remember!**

When the independent variable changes by a constant amount,

- linear functions have constant first differences.
- quadratic functions have constant second differences.
- exponential functions have a constant ratio.

Examples:

linear

$$y = 3x + 4$$

|   |    |    |   |   |    |
|---|----|----|---|---|----|
| x | -2 | -1 | 0 | 1 | 2  |
| y | -2 | 1  | 4 | 7 | 10 |

+3 +3 +3 +3

Quadratic

|   |    |    |    |   |   |
|---|----|----|----|---|---|
| x | -2 | -1 | 0  | 1 | 2 |
| y | -6 | -6 | -4 | 0 | 6 |

+0 +2 +4 +6  
+2 +2 +2

Expo

$$y = 2(5)^x$$

|   |      |     |   |    |
|---|------|-----|---|----|
| x | -2   | -1  | 0 | 1  |
| y | 0.08 | 0.4 | 2 | 10 |

(5) (5) (5)

Is the table linear, quadratic or exponential?

| x | y  |
|---|----|
| 1 | 5  |
| 2 | 9  |
| 3 | 13 |
| 4 | 17 |
| 5 | 21 |

| x | y  |
|---|----|
| 1 | 0  |
| 2 | -1 |
| 3 | 0  |
| 4 | 3  |
| 5 | 8  |

| x | y   |
|---|-----|
| 1 | 3   |
| 2 | 9   |
| 3 | 27  |
| 4 | 81  |
| 5 | 243 |

*Handwritten annotations:*  
For the middle table, a bracket groups the y-values from x=2 to x=5 with a '2' next to it, and another bracket groups the y-values from x=3 to x=5 with a '3' next to it.  
For the right table, a bracket groups the y-values from x=1 to x=5 with a '(3)' next to it.

*Handwritten labels:*  
L      Q      E



Write a function to represent the following table...

| E-mail forwarding |  |
|-------------------|--|
| Time (Days)       | Number of People Who Received the E-mail |
| 0                 | 8  |
| 1                 | 56                                       |
| 2                 | 392                                      |
| 3                 | 2744                                     |

$$y = 8(7)^x$$

Now, predict the number of people who received the email after a week...

6,588,344 People

Write a function to represent the following table...

| Oven Temperature |     |     |     |     |
|------------------|-----|-----|-----|-----|
| Time (min)       | 0   | 10  | 20  | 30  |
| Temperature (°F) | 375 | 325 | 275 | 225 |

-50   -50   -50

$$y = -5x + 375$$

What would you expect the temperature of the oven to be in an hour?

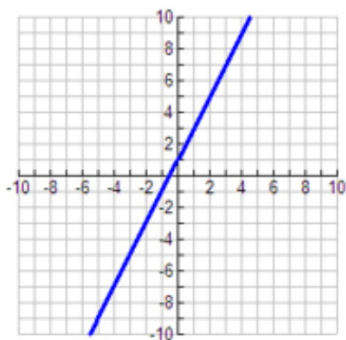
60 min

75°F

## Identifying from a graph...

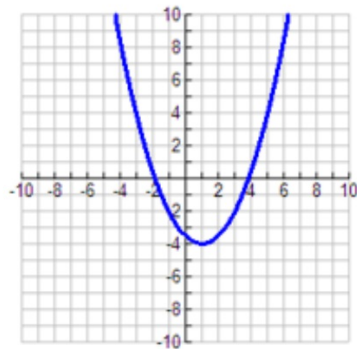
### Linear

Makes a straight line



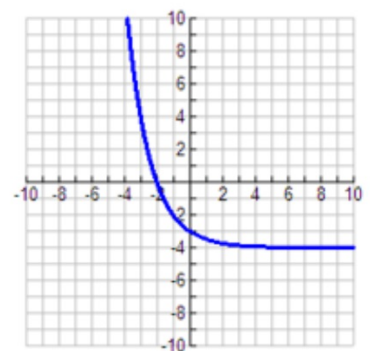
### Quadratic

Makes a U or  $\cap$



### Exponential

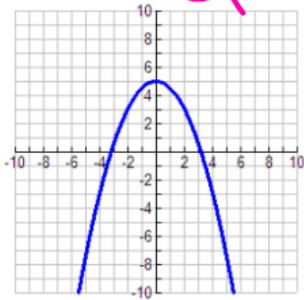
Rises or falls quickly in one direction



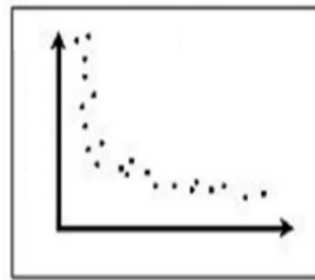
# LINEAR, QUADRATIC or EXPONENTIAL?

Q

a)

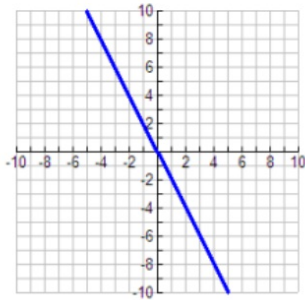


b)



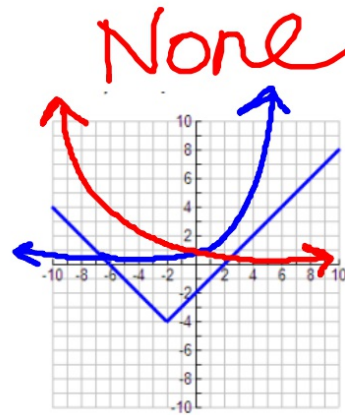
E

c)



L

d)



None