

Warm Up

4/25/19

1. Simplify: $(3x - 4)^2$

$$(3x-4)(3x-4)$$

$$\begin{array}{r} 3x \quad - 4 \\ \hline 3x \quad | \quad 9x^2 \quad - 12x \\ -4 \quad | \quad -12x \quad 16 \\ \hline 9x^2 - 24x + 16 \end{array}$$

2. Simplify: $(3x^2)^2 = \boxed{9x^4}$

3. The $\boxed{\text{sum}}$ of three consecutive even integers is $\boxed{= 144}$. Find the sum of the smaller two integers.

$$x \quad \boxed{46} \quad x + x + 2 + x + 4 = 144$$

$$x + 2 \quad \boxed{48}$$

$$x + 4 \quad \boxed{50}$$

$$\begin{array}{r} 3x + 16 = 144 \\ -16 \quad -16 \\ \hline 3x = 138 \end{array}$$

$$x = 46$$

$$\boxed{94}$$

Directions: Simplify the following polynomials.

- $a(3a + 7) = \underline{3a^2 + 7a}$
- $-2m(m^2 + 6m - 1) = \underline{-2m^3 - 12m^2 + 2m}$
- $4x^3y(x^2 - 2y) = \underline{4x^5y - 8x^3y^2}$

$$\frac{3a^2}{a} \quad \frac{7a}{a}$$

What is FACTORING???

$$\frac{4x^2}{2x} - \frac{2x}{2x}$$

Simplest Form

$$2x(2x - 1)$$

Factored Form

Polynomials that cannot be factored are called

PRIME

Factoring a GCF

Steps for Factoring a GCF:

Step 1: Identify the GCF of the polynomial:

- Check the **coefficients** for a GCF.
- Now look at the **variables**. A variable must be present in all terms to be a GCF. If a variable is present in all terms, take the one with the smallest exponent.

Step 2: Divide each term by the GCF and leave the remaining factors in parentheses

Step 3: Check your work by distributing!

It's like the opposite of distributing!

EXAMPLES:

$$\frac{3x+12}{3}$$
$$3(x+4)$$

$$\frac{6a^2+27}{3}$$
$$3(2a^2+9)$$

EXAMPLES:

$$\frac{15a^2b}{15ab} - \frac{30ab}{15ab}$$
$$15ab(a-2)$$

$$ab - a$$

$$a(b-1)$$

$$5x - 13y$$

PRIME

$$\frac{2x^2y}{2xy} - \frac{2xy^2}{2xy} + \frac{4xy}{2xy}$$
$$2xy(x-y+2)$$

EXAMPLES:

$$6y^4 + 14y^3 - 10y^2$$

$$14gh^2 + 28gh + 14h$$

$$m^3n - m^2n^2 + 5mn^3$$

$$35a^2 - 20ab^2 + 15a$$

4 Terms

Factor by GROUPING

Steps	Example
Step 1: Group the first two terms together and the last two terms together.	$\frac{x^3 + 7x^2}{x^2} \left(\frac{2x + 14}{2} \right)$
Step 2: Factor out the GCF from each binomial.	$\cancel{x^2}(x+7)\cancel{2}(x+7)$
Step 3: Factor the common binomial out.	$(x^2+2)(x+7)$
Step 4: Distribute to check your answer.	$x^3 + 7x^2 + 2x + 14$

Examples:

$$\left(\frac{x^3}{x^2} + \frac{4x^2}{x^2} \cancel{+ 8x + 32} \right)$$
$$\frac{(x^2)(x+4) \cancel{(8)}(x+4)}{(x^2+8)(x+4)}$$

$$\left(w^3 + 5w^2 \cancel{- 8w - 40} \right)$$
$$\frac{(w^2)(w+5) \cancel{(8)}(w+5)}{(w^2-8)(w+5)}$$

Examples:

$$(p^5 - 6p^3 - 2p^2 + 12)$$
$$\cancel{(p^3)}(p^2 - 4) \cancel{- 2}(p^2 - 4)$$
$$(p^3 - 2)(p^2 - 4)$$

$$(3x^3 - 21x^2) + 4x - 28$$
$$\cancel{3x^2}(x - 7)\cancel{4}(x - 7)$$
$$\boxed{(3x^2 + 4)(x - 7)}$$

Examples:

$$(16a^3 + 8a^2 - 6a - 3)$$
$$\cancel{8a^2}(2a+1)\cancel{-3}(2a+1)$$
$$\boxed{(8a^2-3)(2a+1)}$$

$$\left(\frac{8x^2}{4x} + \frac{12x}{4x}\right) + 2xy + 3y$$
$$\cancel{4x}(2x+3)\cancel{y}(2x+3)$$
$$\boxed{(4x+y)(2x+3)}$$

Examples:

$$\frac{\left(\frac{a^3}{a^2} + \frac{a^2b}{a^2}\right)\left(\frac{ab}{b} + \frac{b^2}{b}\right)}{(a^2)(a+b)b(a+b)}$$
$$(a^2+b)(a+b)$$

$$\underline{2xy + 5x - x^2 - 10y}$$

$$\frac{(2xy - 10y)}{2y} + 5x - x^2$$

$$\frac{2y(x-5)}{2y} - x(-5+x)$$
$$(2y-x)(x-5)$$