

1. Two groups of teenagers and adults went to a basketball game last week. The first group paid \$88 for 4 teens and 2 adults. The second group paid \$164 for 7 teens and 4 adults. What was the cost for a teen's ticket and for an adult ticket?

$x = \text{teen ticket}$ $y = \text{adult ticket}$

$$\begin{array}{r} -2(4x + 2y = 88) \\ 7x + 4y = 164 \\ \hline -8x - 4y = -176 \\ + \quad 7x + 4y = 164 \\ \hline -x = -12 \\ \underline{-1} \quad \underline{-1} \\ x = 12 \end{array}$$

$x = \$12$

$$\begin{array}{r} 4(12) + 2y = 88 \\ 48 + 2y = 88 \\ -48 \quad -48 \\ \hline 2y = 40 \\ y = 20 \end{array}$$

$y = \$20$

2. Write each equation in slope-intercept form:

$$\begin{array}{r} -9x + 4y = -24 \\ +9x \quad +9x \\ \hline 4y = 9x - 24 \\ \underline{4} \quad \underline{4} \quad \underline{4} \\ y = \frac{9}{4}x - 6 \end{array}$$

$$\begin{array}{r} 10x - 2y = 14 \\ -10x \quad -10x \\ \hline -2y = -10x + 14 \\ \underline{-2} \quad \underline{-2} \quad \underline{-2} \\ y = 5x - 7 \end{array}$$

3. What is the equation of the line that passes through the points $(-3, 6)$ and $(4, 27)$?

$$m = \frac{27-6}{4-(-3)} = \frac{21}{7} = 3$$

$$y = mx + b$$

$$27 = 3(4) + b$$

$$27 = 12 + b$$

$$\underline{-12} \quad \underline{-12}$$

$$b = 15$$

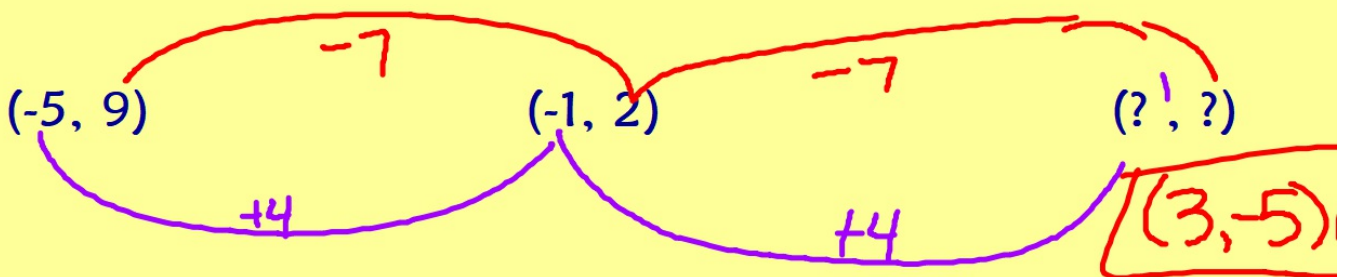
$$y = 3x + 15$$

Midpoint and Distance Formula Application

Missing Endpoint

*Use when given 1 endpoint and the midpoint to find the other endpoint

"Swoop Swoop Method"



1. Swoop from -5 to -1

2. Swoop the same distance from -1 to the unknown x-value

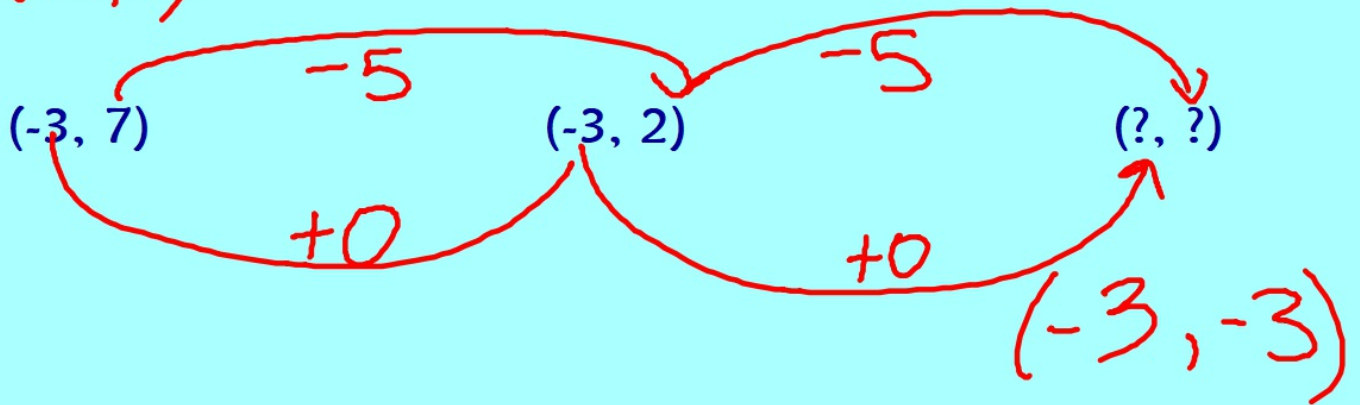
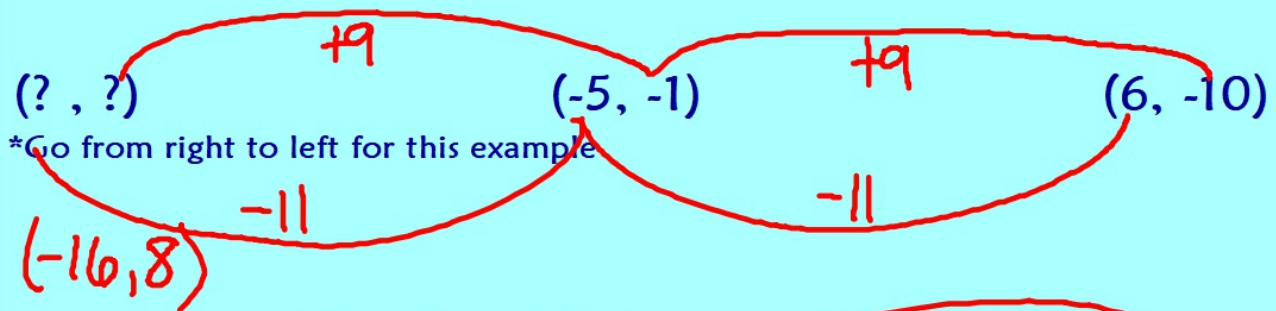
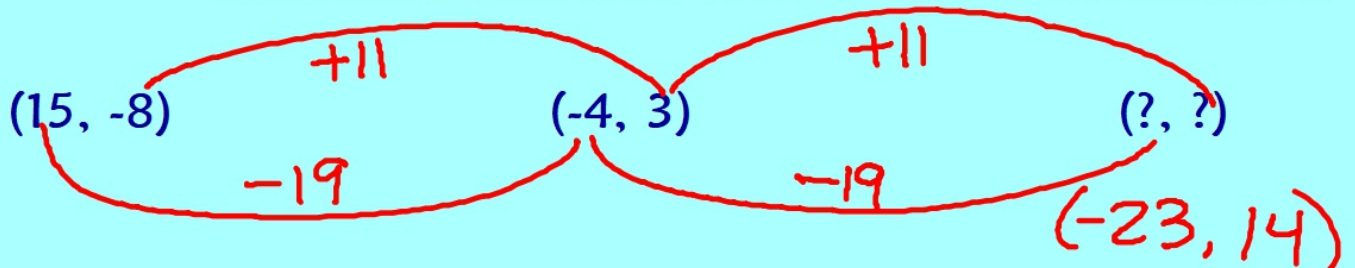
$$-1 + 4 = 3 \text{ (Endpoint has x-value of 3)}$$

3. Swoop from 9 to 2

4. Swoop the same distance from 2 to the unknown y-value

$$2 - 7 = -5 \text{ (Endpoint has y-value of -5)}$$

More Examples (Use the Swoop Swoop Method)



$$(-4, 7) \quad (3, 12)$$

$$\left(\frac{-4+3}{2}, \frac{7+12}{2}\right)$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \quad \left(-\frac{1}{2}, \frac{19}{2}\right)$$

$$d = \sqrt{(3+4)^2 + (12-7)^2} \quad (-0.5, 9.5)$$

$$\sqrt{(7)^2 + (5)^2}$$

$$\sqrt{49+25} = \boxed{\sqrt{74}} = \boxed{8.6}$$

$$(6, 7) \quad (-3, 9)$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \quad \left(\frac{6+3}{2}, \frac{7+9}{2}\right)$$

$$\sqrt{(-3-6)^2 + (9-7)^2} \quad \left(\frac{3}{2}, 8\right)$$

$$\sqrt{(-9)^2 + (2)^2}$$

$$\sqrt{81+4} = \boxed{\sqrt{85}} = 9.23$$