

Warm-Up

5/9/19

Solve:

$$1. \ x^2 - 10x + 21 = 0$$

$$\frac{ac=21}{-3|-7}$$

$$(x^2 - 3x)(-7x + 2) = 0$$

$$x(x-3) - 7(x-3) = 0$$

$$(x-7)(x-3) = 0$$

$$x-7=0 \quad x-3=0$$

~~$$2. \ 9x^2 = 36$$~~

~~$$-36 -36$$~~

$$9x^2 - 36 = 0$$

$$9(x^2 - 4) = 0$$

~~$$9(x+2)(x-2) = 0$$~~

~~$$x+2=0 \quad x-2=0$$~~

$$\{3, 7\}$$

$$\{-2, 2\}$$

$$3. \ y = 3x^2 + 6x - 45$$

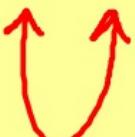
$$a = 3 \quad b = 6 \quad c = -45$$

$$x = -1$$

$$\text{Roots: } \{-5, 3\}$$

$$3(x^2 + 2x - 15)$$

$$\frac{ac=-15}{-3|5}$$



$$\text{Vertex } (-1, -48)$$

Min or Max?

$$y = 3(-1)^2 + 6(-1) - 45$$

$$3 - 6 - 45$$

$$-3 - 45 = -48$$

$$(x^2 - 3x)(5x - 15) = 0$$

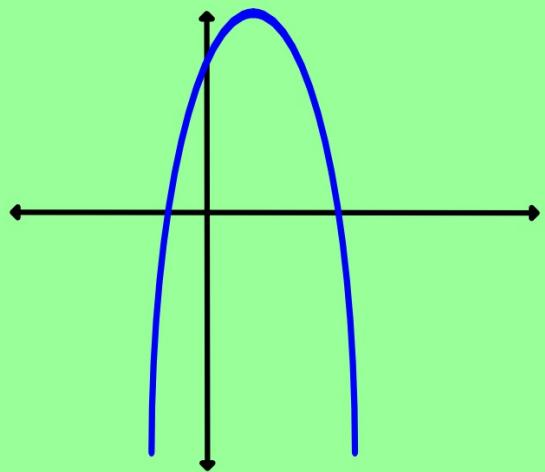
$$x(x-3) \cdot 5(x-3) = 0$$

$$(x+5)(x-3) = 0$$

$$x+5=0 \quad x-3=0$$

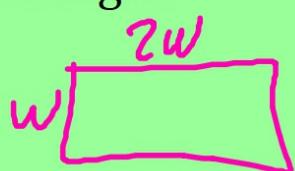
$$\{-5, 3\}$$

Quadratic Equations: Area & Square of a Number Application



Area Application Problems

1. The length of a rectangle is 2 times its width. The area of the rectangle is 72 square inches. Find the dimensions of the rectangle.



$$w(2w) = 72$$

$$\begin{array}{r} 2w^2 = 72 \\ -72 \quad -72 \\ \hline 2w^2 - 72 = 0 \end{array}$$

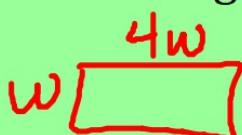
$$2(w^2 - 36) = 0$$

$$\cancel{2}(w+6)(w-6) = 0$$

$$\cancel{w+6} = 0 \quad w-6 = 0$$

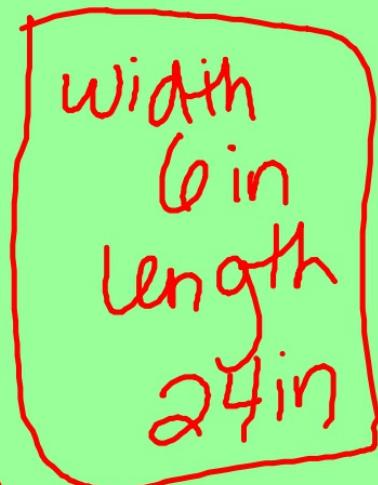
Width
6 in
length
12 in

2. The length of a rectangle is 4 times its width. The area of the rectangle is 144 square inches. Find the dimensions of the rectangle.



$$\begin{aligned} w(4w) &= 144 \\ 4w^2 &= 144 \\ -144 &\quad -144 \\ \hline 4w^2 - 144 &= 0 \end{aligned}$$

$$\begin{aligned} \cancel{4}(w^2 - 36) &= 0 \\ (w+6)(w-6) &= 0 \\ w+6 = 0 &\quad w-6 = 0 \\ w &\neq -6 \quad w = 6 \end{aligned}$$



You Try:

1. The width of a rectangle is 5 meters less than its length. The area is 84 square meters. Find the dimensions of the rectangle.

2. The length of a rectangle is twice the width. The area is 50 square inches. Find the dimensions of the rectangle.

Square of a number

1. Eight more than the square of a number is the same as 6 times the number. Find the number.
- Mult. x

$$\begin{array}{r} 8 + x^2 = 6x \\ -6x \quad -6x \\ \hline x^2 - 6x + 8 = 0 \end{array} \quad ac=8 \quad -4|-2$$

$$(x^2 - 4x)(-2x + 8) = 0$$

$$x(x-4) - 2(x-4) = 0$$

$$(x-2)(x-4) = 0$$

$$x-2=0 \quad x-4=0$$

$$\boxed{x=2}$$

$$\boxed{x=4}$$

2. Fifteen less than the square of a number is the same as twice the number. Find the number.

$$2 \quad x$$

$$\begin{array}{r} x^2 - 15 = 2x \\ -2x \quad -2x \\ \hline x^2 - 2x - 15 = 0 \end{array}$$

$$\begin{array}{r} ac = -15 \\ -5 \mid 3 \end{array}$$

$$(x^2 - 5x)(3x - 15) = 0$$

$$x(x-5) 3(x-5) = 0$$

$$(x+3)(x-5) = 0$$

$$x+3=0 \quad x-5=0$$

$$\boxed{x=-3} \quad \boxed{x=5}$$

x + $2x^2$ = 6
 3. If a number is added to twice its square, the result is 6.
 Find the number.

$$2x^2 + x = 6$$

$$ac = -12$$

$$4 \sqrt{-3}$$

$$2x^2 + x - 6 = 0$$

$$(2x^2 + 4x)(3x - 6) = 0$$

$$2x(x+2) - 3(x+2) = 0$$

$$(2x-3)(x+2) = 0$$

$$\begin{array}{r} 2x-3=0 \\ +3+3 \\ \hline 2x=3 \end{array}$$

$$\begin{array}{l} x+2=0 \\ x=-2 \end{array}$$

$$\boxed{x=3, -2}$$

4. Seven less than 4 times the square of a number is 18.
Find the number.

$$\begin{aligned}4x^2 - 7 &= 18 \\-18 &\quad -18 \\ \hline 4x^2 - 25 &= 0 \\(2x+5)(2x-5) &= 0 \\2x+5=0 &\quad 2x-5=0 \\-5-5 &\quad +5+5 \\ \hline 2x=-5 &\quad 2x=5\end{aligned}$$

$$\boxed{x = -\frac{5}{2}} \quad \boxed{x = \frac{5}{2}}$$

Complete #1 - 4 on the
AREA PRACTICE
worksheet