

1. Solve: $-2(3x + 4y = 24)$
 $6x + 8y = 24$

$$\begin{array}{r}
 \cancel{-6x} - \cancel{8y} = -48 \\
 + \quad \cancel{6x} + \cancel{8y} = 24 \\
 \hline
 0 = -24
 \end{array}$$

$\boxed{\emptyset}$

2. Solve: $-4x + 5 > 29$

$$\begin{array}{r}
 \cancel{-5} - \cancel{5} \\
 \hline
 -4x > 24 \\
 \hline
 \quad -4 \quad -4 \\
 \hline
 \boxed{x < -6}
 \end{array}$$

3. Solve for y.

$$\begin{array}{r}
 \cancel{3x} - 2y < -26 \\
 \hline
 \cancel{-3x} \quad \quad \quad -3x \\
 \hline
 -2y < \cancel{-3x} - 26 \\
 \hline
 \quad -2 \quad \quad -2 \quad -2 \\
 \hline
 \boxed{y > \frac{3}{2}x + 13}
 \end{array}$$

SYSTEMS APPLICATION

Systems Word Problems

DEFINE
VARIABLES!



SET UP EQUATIONS
& SOLVE!



IDENTIFY
THE ANSWER!

1. The ⁺sum of two numbers is 30 and their ⁻difference is 12. Find the two numbers.

$x = 1^{\text{st}} \#$

$y = 2^{\text{nd}} \#$

$$\begin{array}{r} x + y = 30 \\ + \quad x - y = 12 \\ \hline \end{array}$$

$$\begin{array}{r} x + y = 30 \\ - 21 \quad y = -21 \\ \hline y = 9 \end{array}$$

$$\begin{array}{r} 2x = 42 \\ \hline 2 \quad 2 \end{array}$$

$$x = 21$$

21, 9

2. The sum of two numbers is 24 and their difference is 2. What are the numbers?

$$x = 1^{\text{st}} \#$$

$$y = 2^{\text{nd}} \#$$

$$x + y = 24$$

$$x - y = 2$$

3. The difference between two numbers is 9. The first number plus twice the other number is 27. Find the two numbers.

$$x = 1^{\text{st}} \#$$

$$y = 2^{\text{nd}} \#$$

$$x - y = 9$$

$$x + 2y = 27$$

4. The sum of two numbers is 36. Twice the first number minus the second is 6. Find the numbers.

$$x = 1^{\text{st}} \#$$

$$y = 2^{\text{nd}} \#$$

$$x + y = 36$$

$$2x - y = 6$$

5. The sum of two numbers is 20. The difference between three times the first number and twice the second is 40. Find the two numbers.

$$x = 1^{\text{st}} \# \quad y = 2^{\text{nd}} \#$$

$$\begin{array}{r} 2(x + y = 20) \\ 3x - 2y = 40 \\ \hline + 2x + 2y = 40 \\ 3x - 2y = 40 \\ \hline 5x = 80 \\ \frac{5}{5} \quad \frac{5}{5} \\ x = 16 \end{array}$$
$$\begin{array}{r} 16 + y = 20 \\ -16 \quad -16 \\ \hline y = 4 \end{array}$$

16, 4

6. The sum of two numbers is 25. One ~~X~~ number is twice the second ^y number plus seven. What are the two numbers?

$x = 1^{\text{st}} \#$ $y = 2^{\text{nd}} \#$

$$\textcircled{x} + y = 25$$

$$x = \textcircled{2y + 7}$$

$$\textcircled{(2y + 7)} + \textcircled{y} = 25$$

$$3y + 7 = 25$$

$$\begin{array}{r} 3y + 7 = 25 \\ -7 \quad -7 \\ \hline \end{array}$$

$$x = 2(6) + 7$$

$$x = 19$$

19, 6

$$\frac{3y = 18}{3} \quad \frac{18}{3}$$

$$y = 6$$

7. The cost of 3 boxes of envelopes and 4 boxes of notebook paper is \$13.25. Two boxes of envelopes and 6 boxes of notebook paper cost \$17. Find the cost of each. Find the cost of each.

$x = \$$ per box of envelopes

$y = \$$ per box of paper

$$3x + 4y = 13.25$$

$$2x + 6y = 17.00$$

8. The cost of 12 oranges and 7 apples is \$5.36. Eight oranges and 5 apples cost \$3.68. Find the cost of each.

$x = \$$ per orange
 $y = \$$ per apple

$$\begin{array}{r} -5(12x + 7y = 5.36) \\ 7(8x + 5y = 3.68) \end{array}$$

$$\begin{array}{r} -60x - 35y = -26.80 \\ + 56x + 35y = 25.76 \end{array}$$

$$\begin{array}{r} -4x = -1.04 \\ \hline -4 \quad -4 \end{array}$$

$$x = \$0.24$$

Orange
\$0.24

$$\begin{array}{r} 8(0.24) + 5y = 3.68 \\ 1.92 + 5y = 3.68 \\ -1.92 \quad -1.92 \end{array}$$

Apple
\$0.35

$$5y = 1.76$$

$$y = \$0.35$$

9. Gabby and Sydney bought some pens and pencils. Gabby bought 4 pens and 5 pencils for \$6.71. Sydney bought 5 pens and 3 pencils for \$7.12. Find the cost of each.

$$\begin{array}{ll} x = \$ \text{ per pen} & 4x + 5y = 6.71 \\ y = \$ \text{ per pencil} & 5x + 3y = 7.12 \end{array}$$

10. At a sale on winter clothing, Cody bought two pairs of gloves and four hats for \$43.00. Tori bought two pairs of gloves and two hats for \$30.00. Find the cost of each.

x = cost per glove set

y = cost per hat

$$\begin{array}{r} \cancel{2x} + 4y = 43.00 \\ \cancel{2x} + 2y = 30.00 \\ \hline \end{array}$$

\$6.50
per
hat

$$\begin{array}{r} 2x + 2(6.50) = 30 \\ 2x + 13 = 30 \\ -13 \quad -13 \\ \hline 2x = 17 \\ \frac{2x}{2} = \frac{17}{2} \end{array}$$

\$8.50
per
pair of
gloves

$$2y = 13.00$$

$$\frac{2y}{2} = \frac{13.00}{2}$$

$$y = \$6.50$$

$$x = \$8.50$$

11. A garden supply store sells two types of lawn mowers. The smaller mower costs \$249.99 and the larger mower cost \$329.99. If 30 total mowers were sold and the total sales for a given year was \$8379.70, find how many of each type were sold.

$x = \#$ of small mower

$y = \#$ of large mower

$$x + y = 30$$

$$249.99x + 329.99y = 8379.70$$

12. The Town Recreation Department ordered a total of 100 baseballs and bats for the summer baseball camp. Baseballs cost \$4.50 each and bats cost \$20 each. The total purchase was \$822. How many of each item was ordered?

$x = \text{baseballs}$

$y = \text{bats}$

$$x + y = 100$$

$$4.50x + 20y = 822$$

13. A group of 40 children attended a baseball game on a field trip. Each child received either a hot dog or bag of popcorn. Hot dogs were \$2.25 and popcorn was \$1.75. If the total bill was \$83.50, how many hotdogs and bags of popcorn were purchased?

$x = \text{hot dogs}$ $y = \text{popcorn bags}$

$$-2.25(x + y = 40)$$

$$2.25x + 1.75y = 83.50$$

$$\begin{array}{r} -2.25x - 2.25y = -90 \\ + \quad 2.25x + 1.75y = 83.50 \\ \hline \end{array}$$

$$\begin{array}{r} -0.50y = -6.50 \\ \hline -0.50 \quad -0.50 \end{array}$$

$$y = 13$$

14. One night a theater sold 548 movie tickets. An adult's ticket costs \$6.50 and a child's ticket cost \$3.50. In all, \$2881 was taken in. How many of each kind of ticket were sold?

$x = \#$ of adult tickets

$y = \#$ of child tickets

$$x + y = 548$$

$$6.50x + 3.50y = 2881$$

15. Adult tickets for the school musical sold for \$3.50 and student tickets sold for \$2.50. On a given night, 321 tickets were sold for \$937.50. How many of each kind of ticket were sold?

x = adult tickets

y = student
tickets

$$\begin{aligned}x + y &= 321 \\ 3.50x + 2.50y &= 937.50\end{aligned}$$

16. A collection of dimes and nickels is worth \$3.30. If there are 42 coins in all, how many of each kind of coin are there?

$d = \text{dimes}$ $n = \text{nickels}$

$$-0.10(d + n = 42)$$

$$0.10d + 0.05n = 3.30$$

$$\begin{array}{r} + \quad -0.10d - 0.10n = -4.20 \\ \quad 0.10d + 0.05n = 3.30 \\ \hline \end{array}$$

$$\begin{array}{r} -0.05n = -0.90 \\ \hline -0.05 \quad -0.05 \end{array}$$

$$n = 18$$

$$18$$

$$d + 18 = 42$$

17. Mary has a collection of nickels and quarters for a total value of \$4.90. If she has 42 coins total, how many of each kind are there?

$$\begin{array}{l} n = \text{nickels} \\ q = \text{quarters} \end{array} \quad \begin{array}{l} -0.05(n + q = 42) \\ 0.05n + 0.25q = 4.90 \end{array}$$

$$\begin{array}{r} + \quad \cancel{-0.05n} - 0.05q = -2.10 \\ \quad \cancel{0.05n} + 0.25q = 4.90 \\ \hline \quad \quad 0.20q = 2.80 \\ \quad \quad \underline{0.20} \quad \underline{0.20} \\ \quad \quad q = 14 \end{array}$$

14 quarters
28 nickels